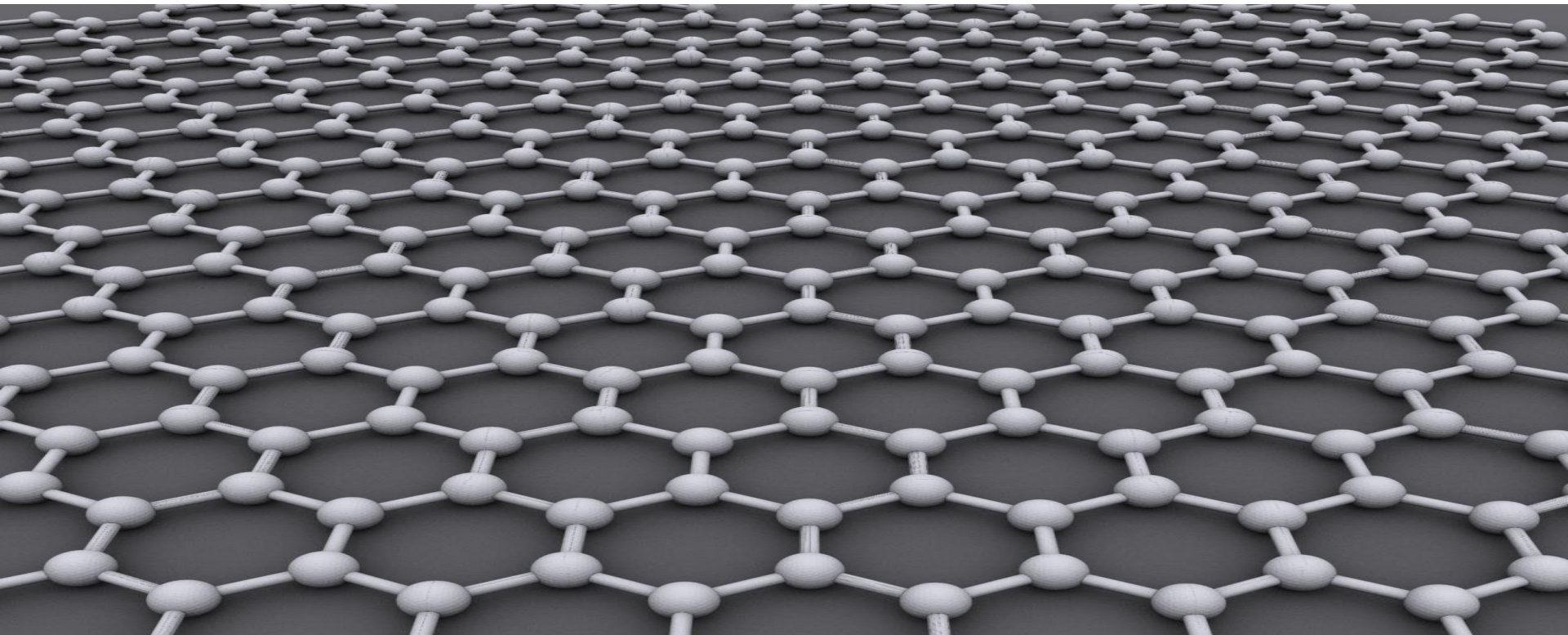


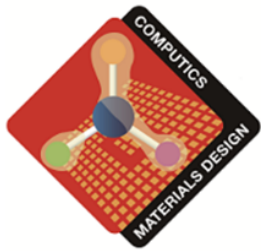
# 第一原理量子状態計算コード“Naniwa”の開発 と研究事例

## Quantum adsorbed states of hydrogen isotope atoms on graphene

H. Nakanishi, H. Kasai

Division of Precision Science & Technology and Applied Physics,  
Graduate School of Engineering, Osaka University, JAPAN





# Material Design through Computics:

Complex Correlation and Non-equilibrium Dynamics

**A02-7: New physical properties and quantum dynamics  
proved by protons and muons (22104008)**

A02-7: プロトン・ミューオンで探る新物性と量子ダイナミクス

ビルデ マーカス@東京大学生産技術研究所

パラジウム(110)表面における水素吸収の機構

Hydrogen absorption mechanism at the palladium (110) surface

後藤英和@大阪大学工学研究科

多体系量子状態計算手法の開発

下司雅章@大阪大学ナノサイエンスデザイン教育センター

$\text{AlH}_3$ の圧力誘起金属-半導体転移及び希土類水化物の高圧下での構造安定性

# 第一原理量子状態計算コード“Naniwa”の開発 と研究事例

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UltraSlow Muon Microscope

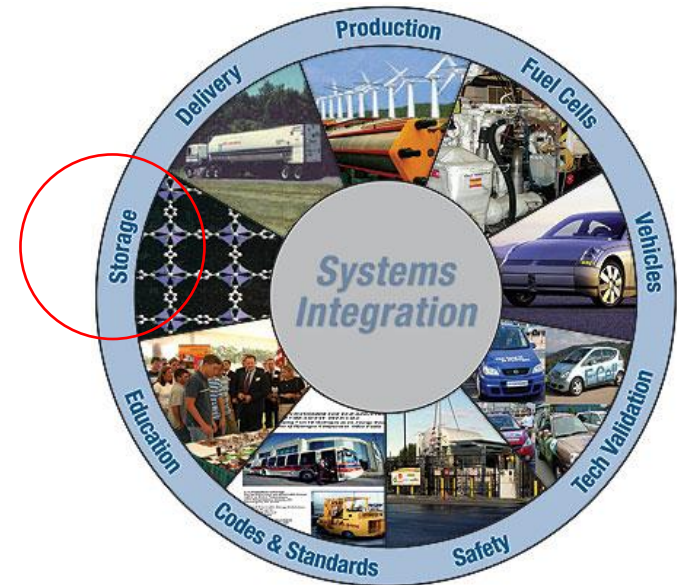
A02:Spin transport and reactions at interface (23108003)

山梨大学 鳥養 映子  
Amba Datt Pant.

## Hydrogen storage technology

It is required for the green hydrogen economy

- **Compressed hydrogen**
- **Liquid hydrogen**
- **Metal Hydride**
- 
- . . . . .



<http://www.hydrogen.energy.gov>

More efficient, safety, economy, moderate condition, environmentally friendly technology are strongly pursued.

Graphite or graphene based hydrogen storage

C:H = 1:1, Hydrogen storage weight ratio is 7.69 w%

Desired target values:

DOE (United States Department of Energy) : Over 6 w% @ under 100°C

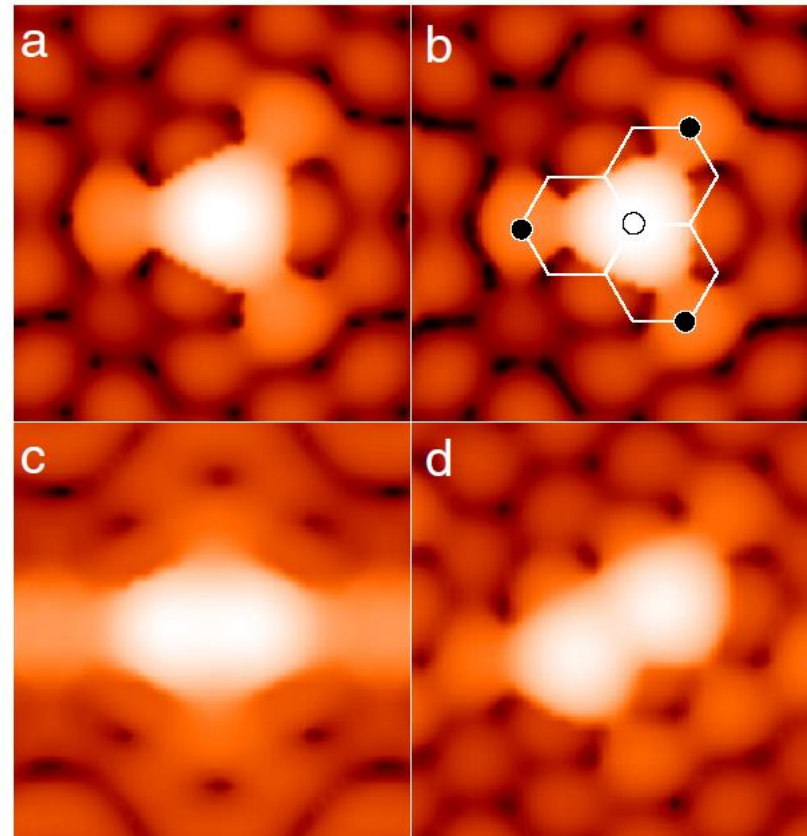
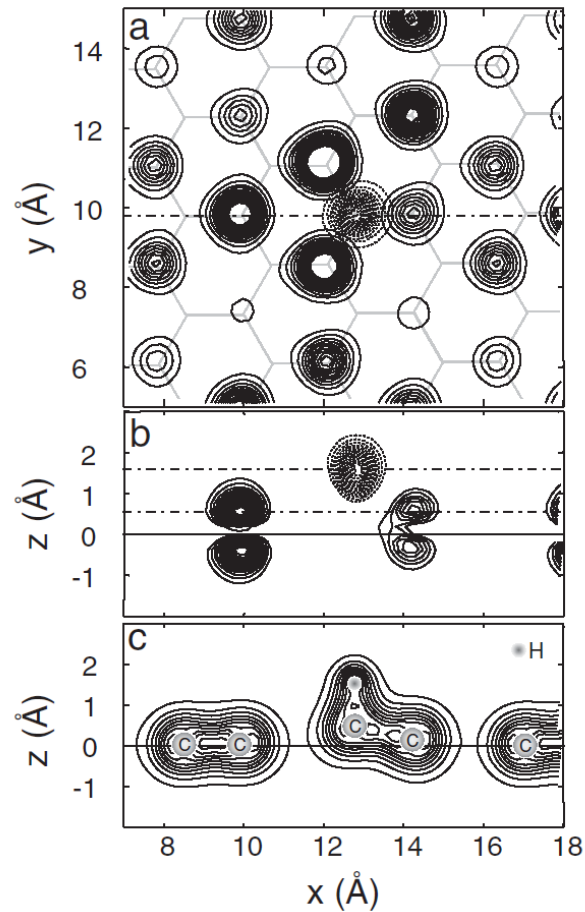
IEA (International Energy Agency) : 5.0 w% @ 80°C



# “Identifying Hydrogen Atoms on Graphite”

T. ROMAN, W. A. DINO, H. NAKANISHI, H. KASAI, K. NOBUHARA, T. SUGIMOTO, and K. TANGE

Journal of the Physical Society of Japan  
Vol. 76, No. 11, November, 2007, 114703



# High-uptake graphene hydrogenation: a computational perspective

T Roman, W A Dino, H Nakanishi and H Kasai

J. Phys.: Condens. Matter 21 (2009) 474219

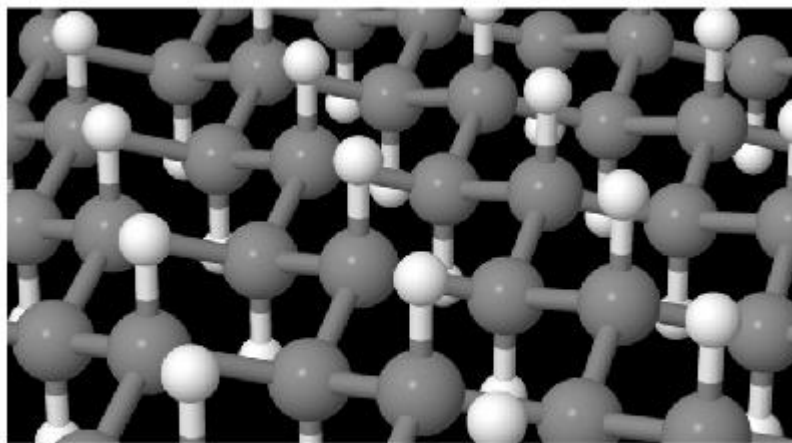
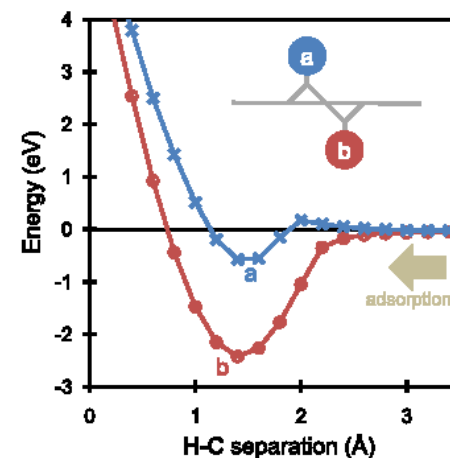
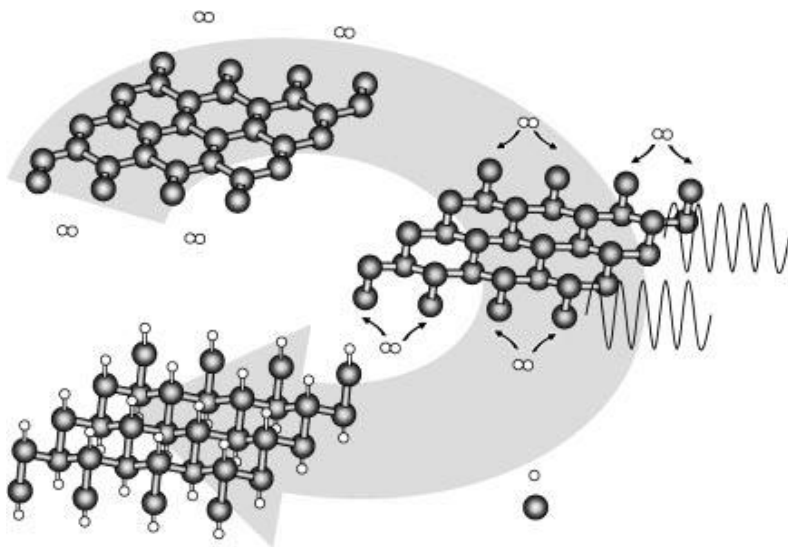


Figure 7. Stable form of fully hydrogenated graphene. Hydrogen atoms are shown in white.



## Realizing a Carbon-Based Hydrogen Storage Material



T. Roman, et al., JJAP. 45,(2006) 1765.

Fig. 1. Sections of fully relaxed structures of graphite (a) before, (b) during, and (c) after hydrogen adsorption. Graphite, as it is, has been shown not to readily react with molecular hydrogen, but dissociative adsorption proceeds when the graphene plane is slightly perturbed (b), initiated by the periodically changing field of infrared radiation. Maximum hydrogen uptake in the final assembly, a diamond-like carbon sheet covered with hydrogen, is shown in (c). The added contribution of the graphite edges in holding hydrogen is not included in these illustrations.

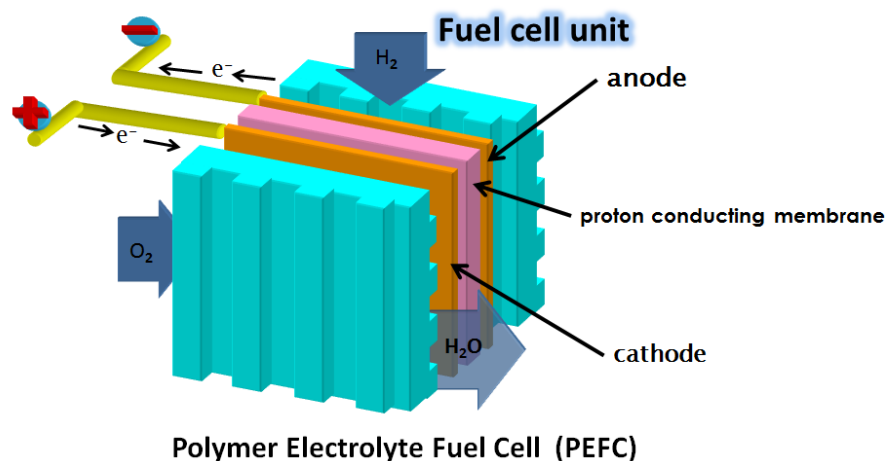
We want to treat the quantum behavior of the hydrogen in the material. Hydrogen is one of the key element for the future technology.

“energy technology”, “biotechnology”



$$M_{\text{Proton}} \gg m$$

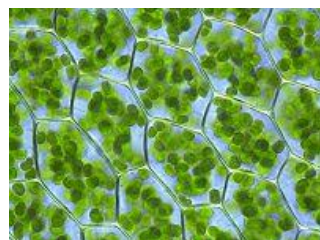
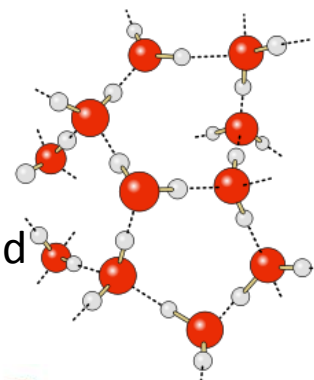
Hydrogen Reactions on Fuel cell anode



electrolyte

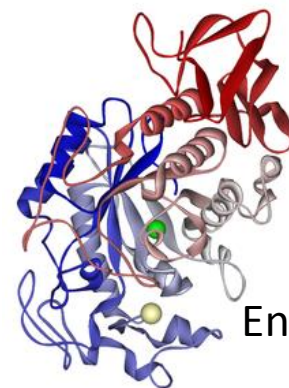
hydrogen bond

aqueous solution



Photosynthesis

biochemistry



Enzyme catalysis

Conventional ab initio simulations can treat electrons by quantum mechanics. We have been developing the quantum simulation code for both the nuclei and electrons, Naniawa: 浪速.

# What is Naniwa ?

- **NANIWA** is a computational code for performing first principles quantum mechanical calculations.
- Two kinds of Naniwa codes in Kasai lab.

*Naniwa for quantum reaction*: It is a quantum mechanical version of the first principles molecular dynamics (MD) calculations, for reactions.

“we can solve the scattering problems, and obtain the probability of some events, adsorption, desorption, reflection, excitation, etc.”

*Naniwa for quantum state*: It is a nucleus version of the first principles quantum state calculations.

“We can solve the eigenvalue problem, and obtain the eigenstates and their eigenenergies for atom (nuclear) motion”



# Our quantum simulation scheme: Naniwa

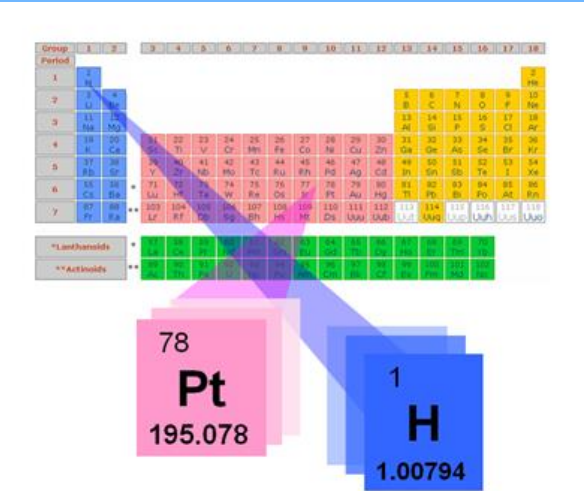
Interactions between nucleus is calculated by DFT based first principle calculations

Potential energy for nucleus motions:  $U_n(\mathbf{R})$

Solve the Schrödinger equation for nucleus motion

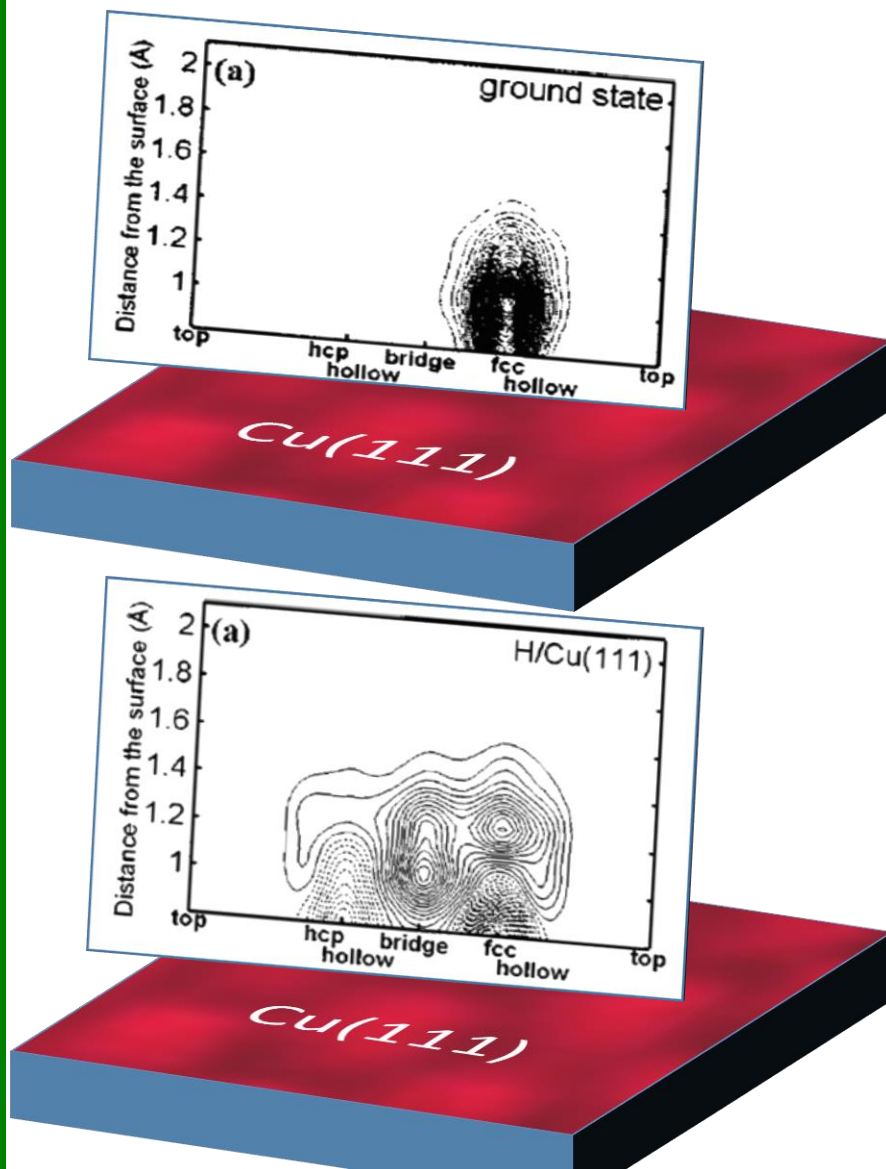
Wave function for nucleus motion

Derive the various physical quantities



- Parameters are only atomic number of elements
- No fitting and no artificial procedure

Calculate the Eigen states  
for the atomic motions



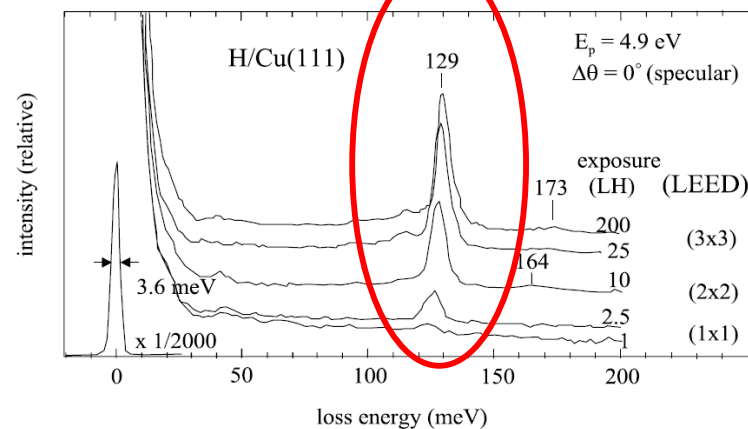
## Surface-normal vibration energy of Hydrogen atom adsorbed on Cu(111) surface

Our simulation result *	135 meV
Experimental data **	129 meV

5% error

\*K. Nobuhara *et al.*, J. Appl. Phys. 96 (2004) 5020.

for Excited state



Electron energy loss spectroscopy (EELS)

\*\*G. Lee, *et al.*, Surf. Sci. **498** (2002) 229.

No fitting parameters !

# Comparison between our simulation Naniwa and experimental results

## Surface-normal vibration excitation energy of hydrogen atom adsorbed on metal surface

	Naniwa	Experiment	Error
H on Cu(111)	135 meV	129 meV*	4.7%
D on Cu(111)	104 meV	96 meV	8.3%
isotope effect	1.29	1.34	3.4%

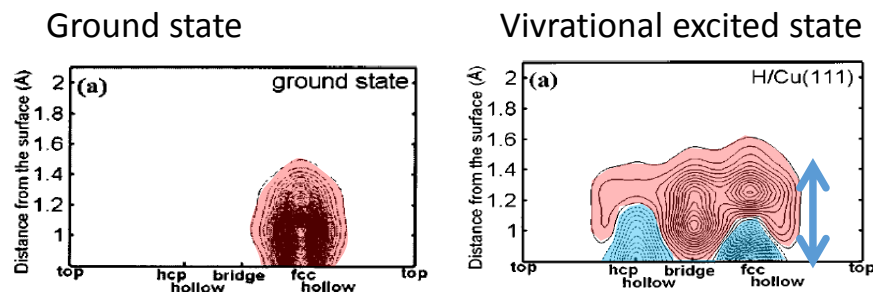
Ratio in harmonic potential is  $\sqrt{2} = 1.414$

\*G. Lee, *et al.*, Surf. Sci. **498** (2002) 229.

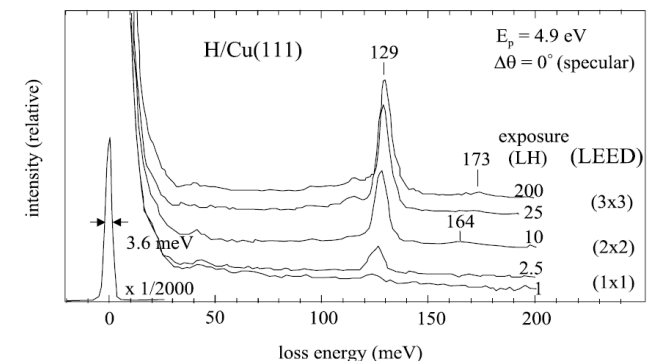
	Naniwa	Experiment	Error
H on Pd(111)	114 meV	124 meV**	8.1%

\*\* H. Conrad, *et al.*, J. Vac. Sci. Technol. A5, 452 (1987).

**Less than 10% error**



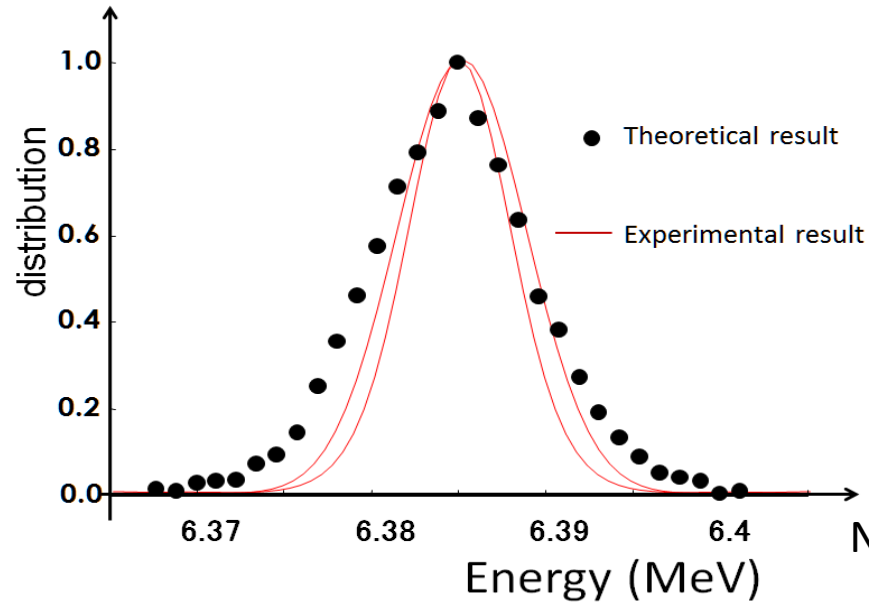
**No fitting parameters !**



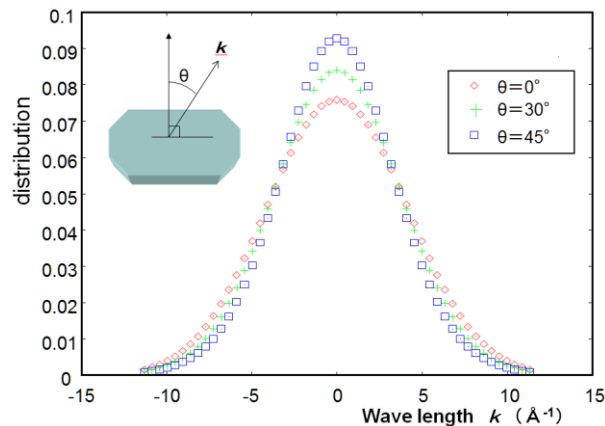
Electron energy loss spectroscopy (EELS)\*

# Comparison between our simulation Naniwa and experimental results

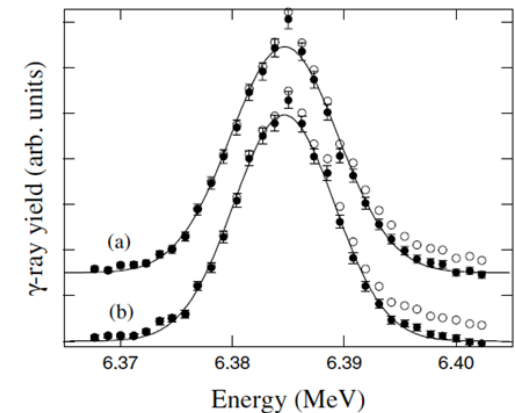
**Momentum distribution of adsorbed hydrogen atom is observable in its ground state.**



NRA : Nuclear Reaction Analysis



**Naniwa**



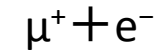
K. Fukutani et al., PRL 48(2002)116101.



# (Positive) muon $\mu^+$

Particle statistics	Fermionic
Mass: $m_\mu$	105.658369(9) MeV/c <sup>2</sup>
Electric charge:	e
Spin:	$1/2$
Mean lifetime : $\tau$	$2.19703(4) \times 10^{-6}$ sec

Positive muon catches an electron, and forms the hydrogen like atom.



Muonium

Its reduced mass and magnetic moment is different from a hydrogen atom.

Isotope of hydrogen

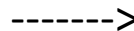
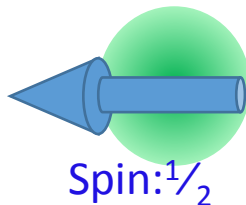
$$m_\mu \sim (1/9) m_p$$

$$\sim 207 m_e$$

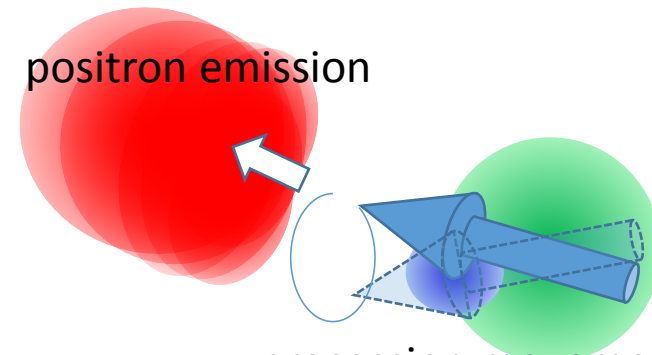
$\mu^+$  Antimuon  $\rightarrow$  positron + Antimuon neutrino + electron neutrino

Life time :  $\tau \sim 2.2 \mu\text{sec}$

**Muon spin spectroscopy :  $\mu\text{SR}$**

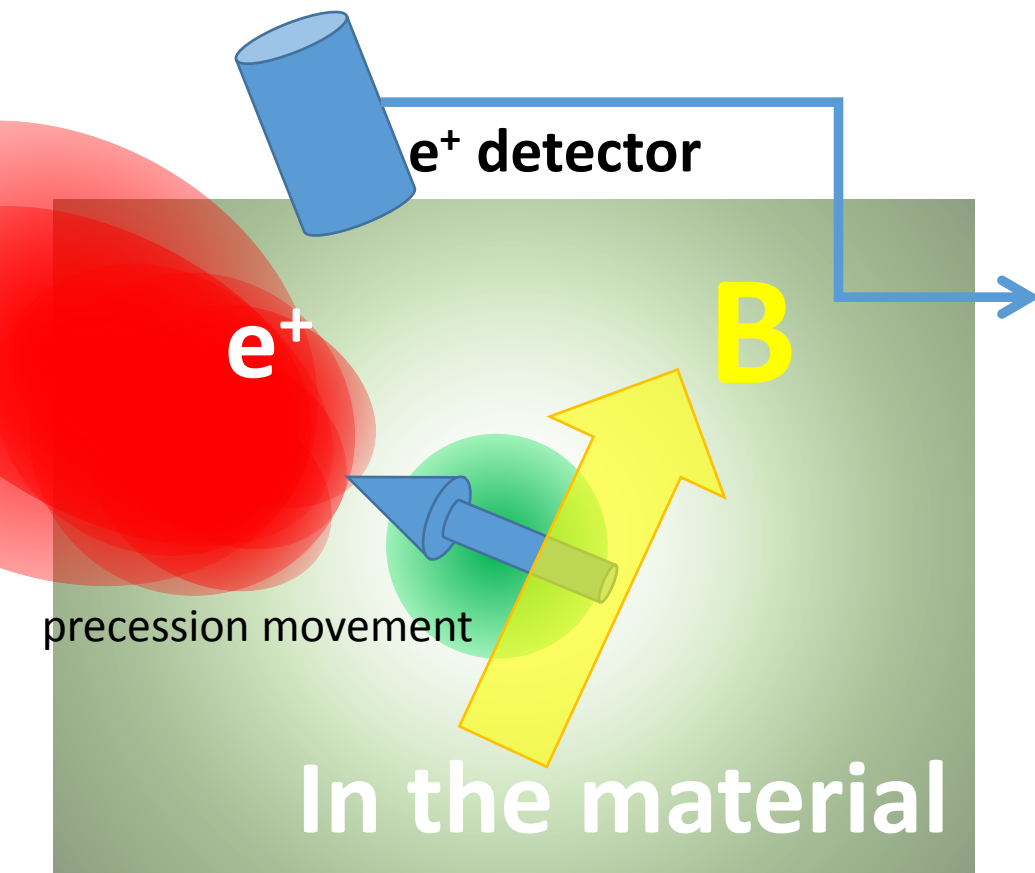


The primary decay mode of a pion is a purely leptonic decay into a muon and a muon neutrino.  
And the muon is 100% spin polarized

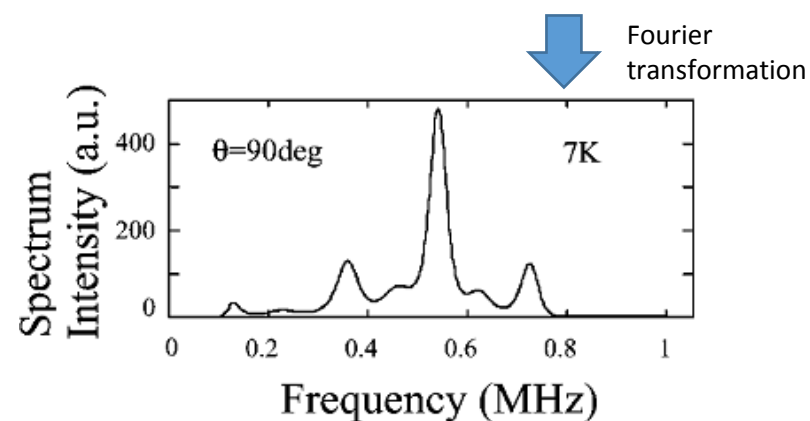
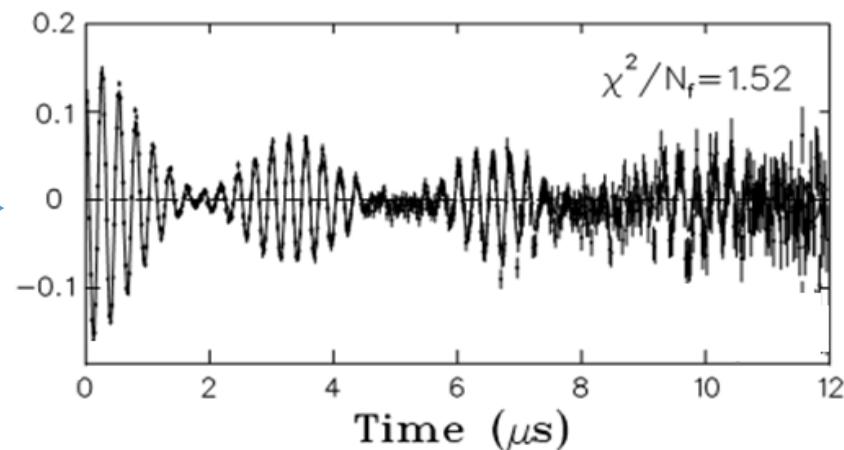


precession movement in the magnetic moment  
sensitive magnetic measurement

Gyromagnetic ratio : 135.53 MHz/T

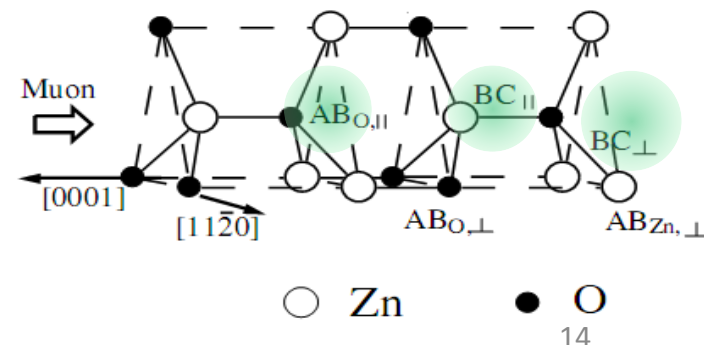


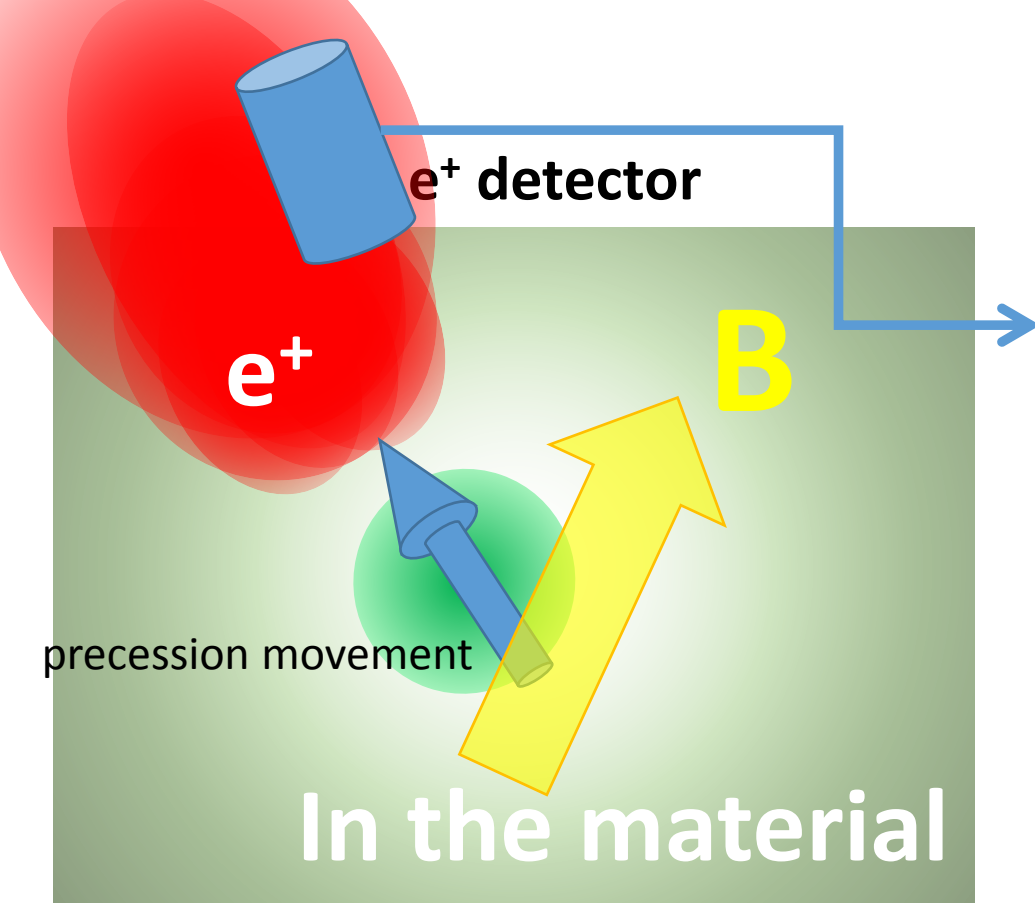
$\mu$ SR time spectrum.



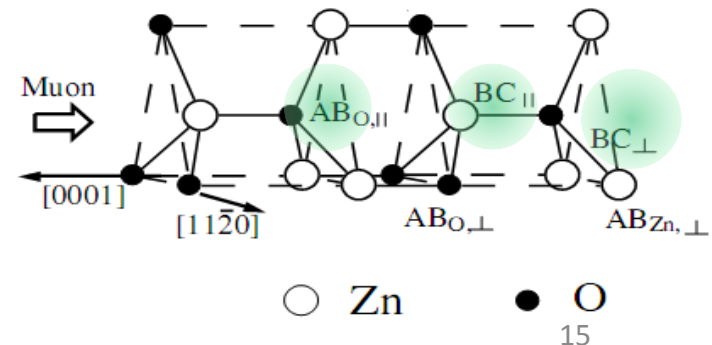
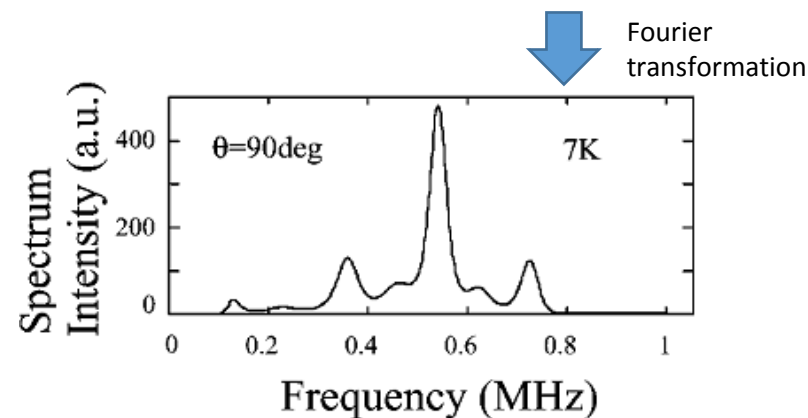
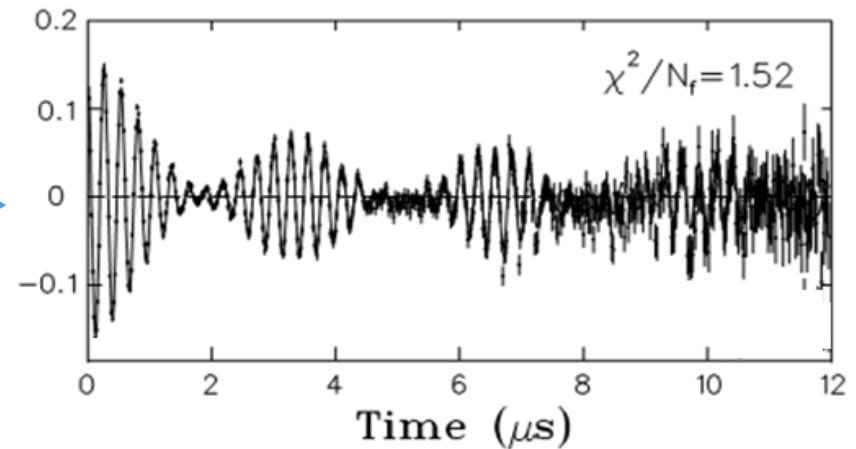
Muon plays as the small-mass proton with a communication function.

We can detect the quantum behaviors of Hydrogen-like particles in material.



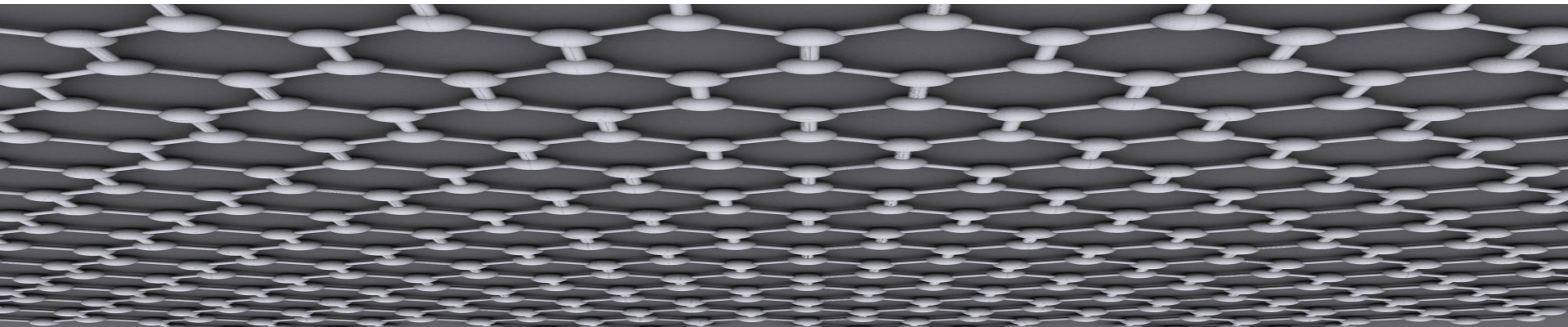


μSR time spectrum.



Muon plays as the small-mass proton with a communication function.

We can detect the quantum behaviors of Hydrogen-like particles in material.



## For electron

Hydrogen coverage:  $1/18 = 5.6\%$

Supercell: Slab model, 3x3 graphene units  
with dipole correction parallel to c-axis

Spin: Polarized calculation

k-sampling points: 5x5x1

GGA: Perdew-Burke-Ernzerhof (PBE)

Vdw: DFT-D2 method of Grimme

Basis set: plane wave

Cut off energy: 400eV

Code Package: VASP 5.2.12



## For nucleus

Supercell: Slab model, 1x1 graphene unit

Potential grid: 20 x 20 x 20

Basis set: 20 x 20 x 20 Gaussians

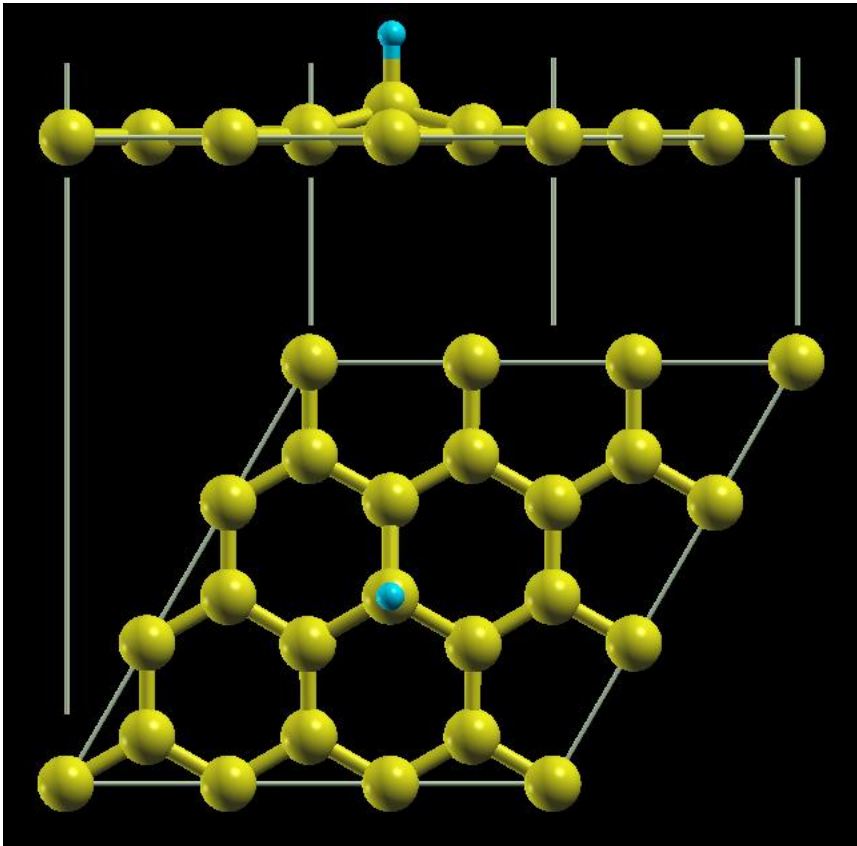
Symmetry Correction in graphene plane

Code Package: Naniwa (Ver. Syk20130524)

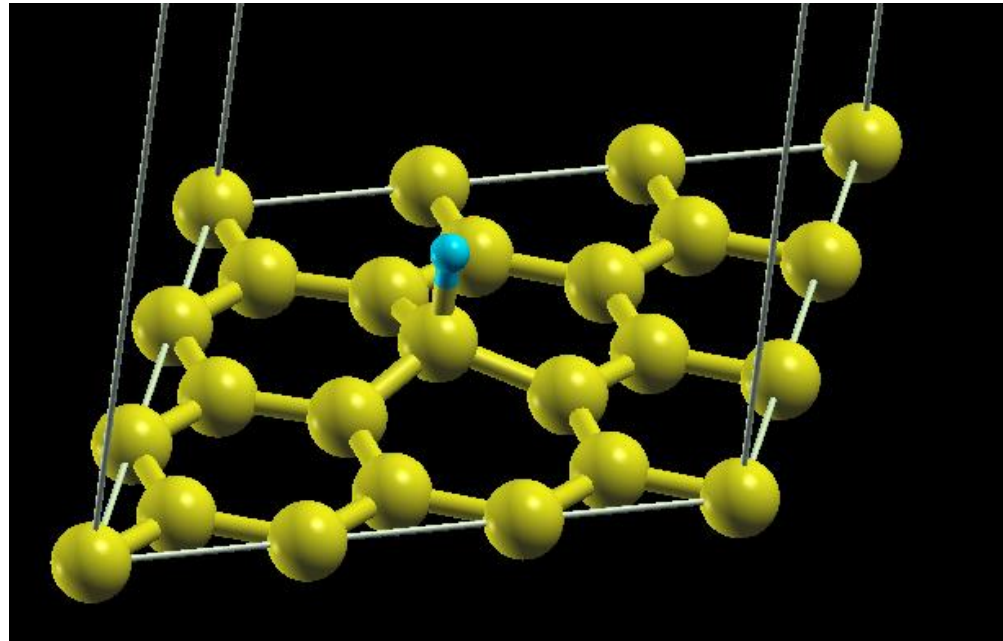




# Classical hydrogen adsorbed structure on graphene



Adsorbed site: Top site  
Adsorbed type: chemisorption  
Adsorbed energy: **-0.816 eV**

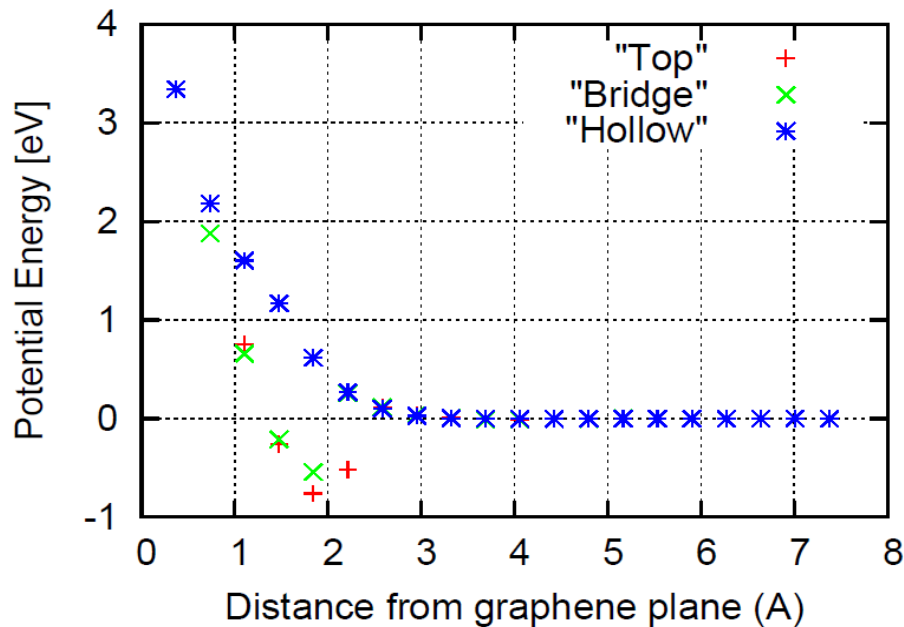


Hydrogen induces the corrugation in graphene structure. And the  $sp^3$ -like covalent bond is formed between hydrogen and carbon atoms.

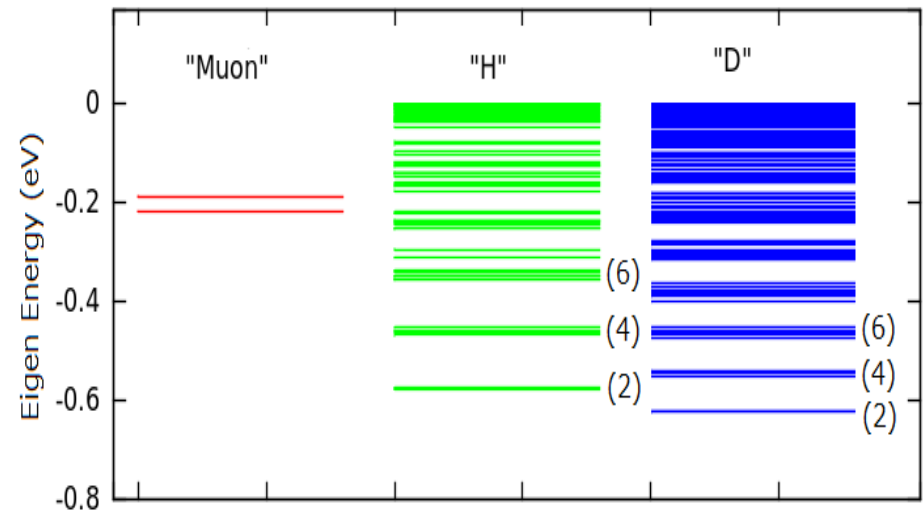
# Relaxed graphene

## Potential energy

Adiabatic potential energy for hydrogen on relaxed graphene



## Naniwa results



Eigen energies of positive muon, proton and deuteron on relaxed graphene

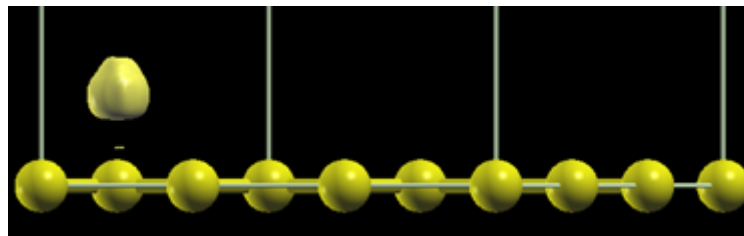
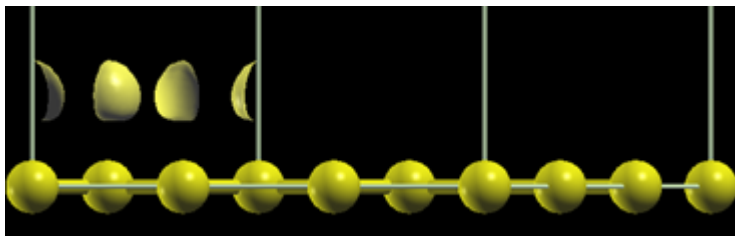
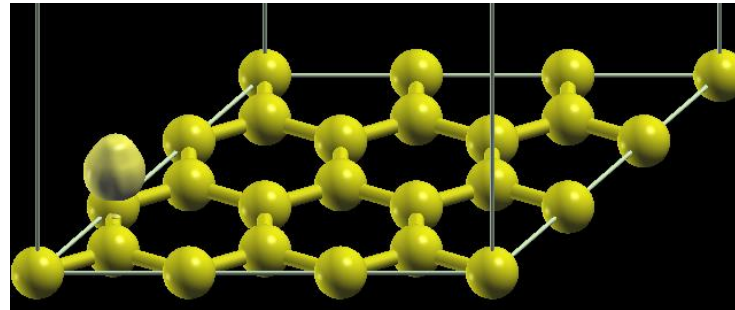
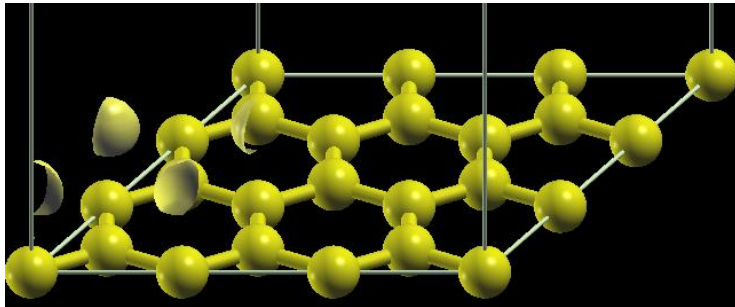
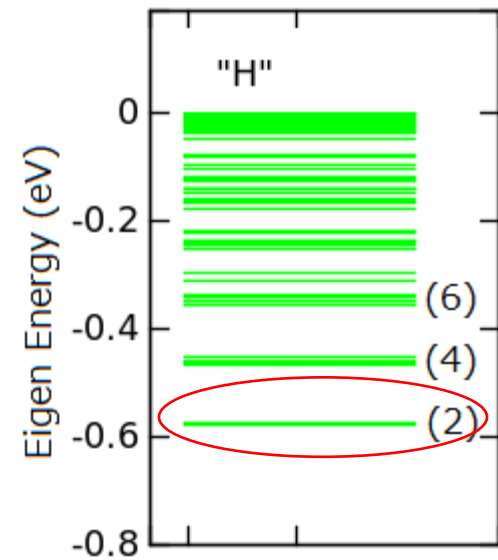
Quantum adsorbed energy of Muon: **-0.22 eV**

Quantum adsorbed energy of proton: **-0.58 eV**

# Wave function of proton in its ground states

Adsorbed energy: **-0.58 eV**

<2 degenerate energy states > in unit cell

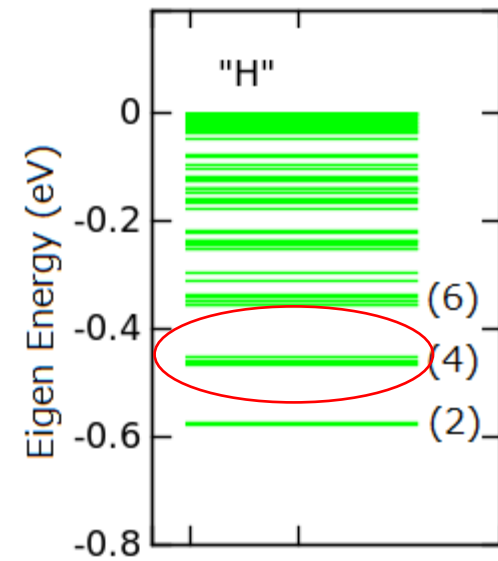
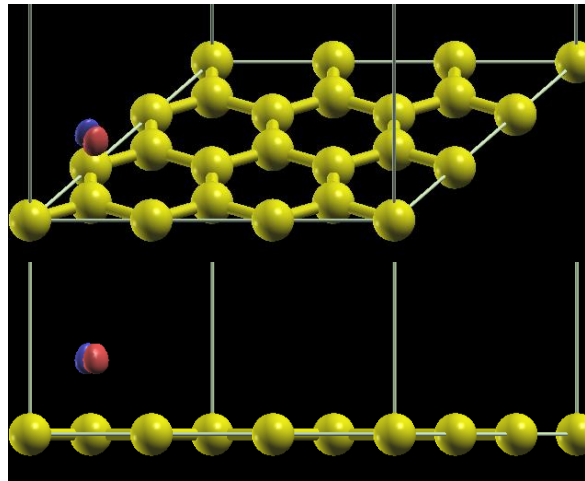
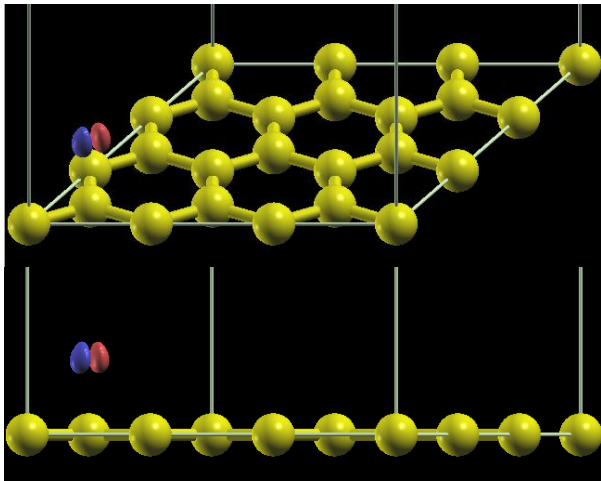
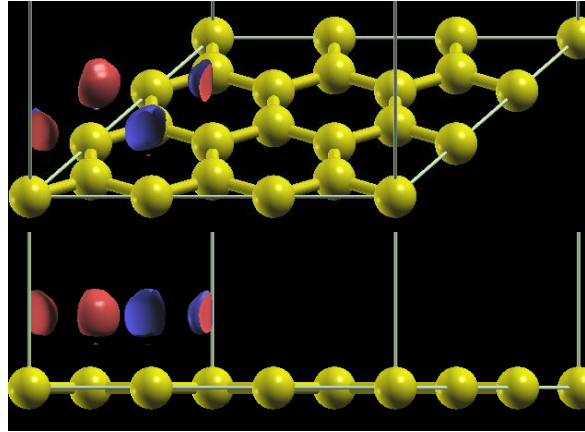
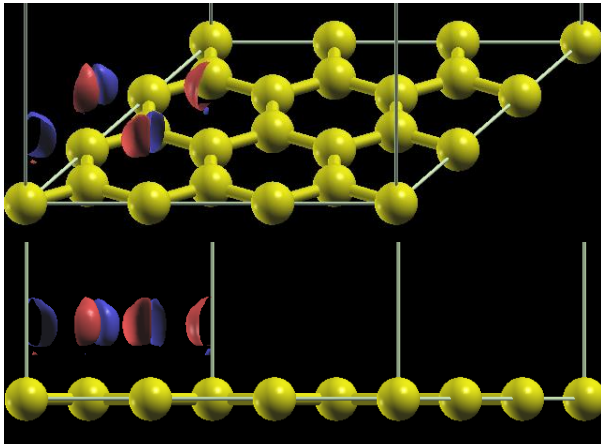


TDS experimental data : **-0.59 eV or -0.65eV**

X. Zhao, et al., J.Chem.Phys. 124(2006)194704

# Wave function of proton in its 1<sup>st</sup> excited states

Vibrational excited parallel to the graphene plane  
<4 degenerate energy states > in unit cell

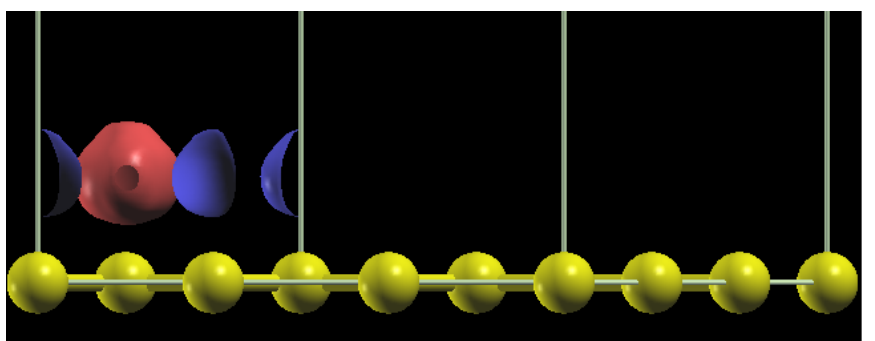
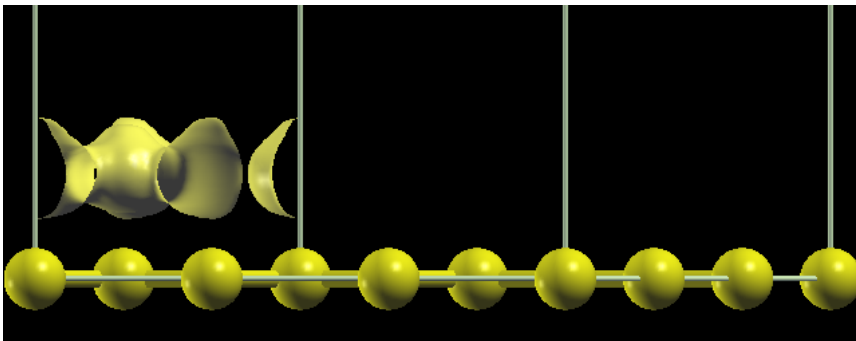
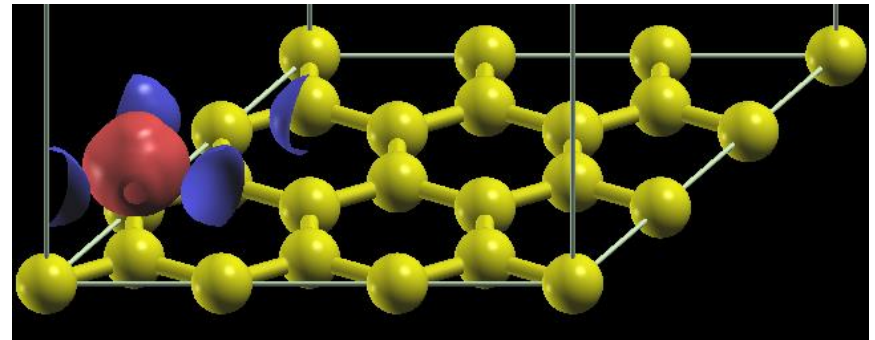
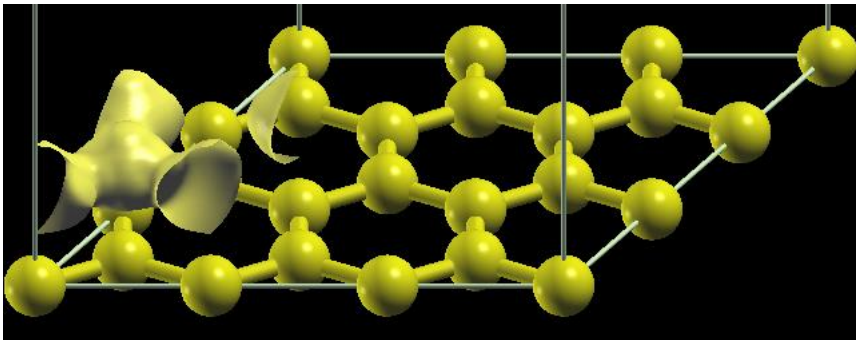
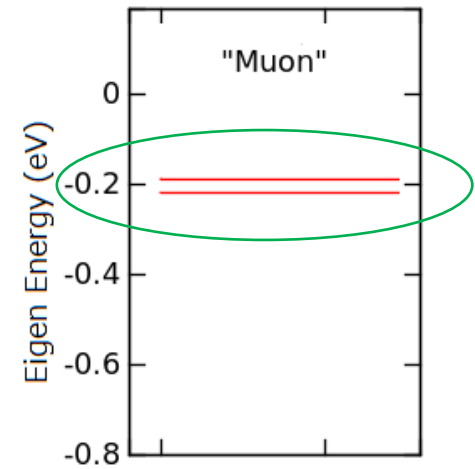




# Wave function of muon in its ground state and 1<sup>st</sup> excited state

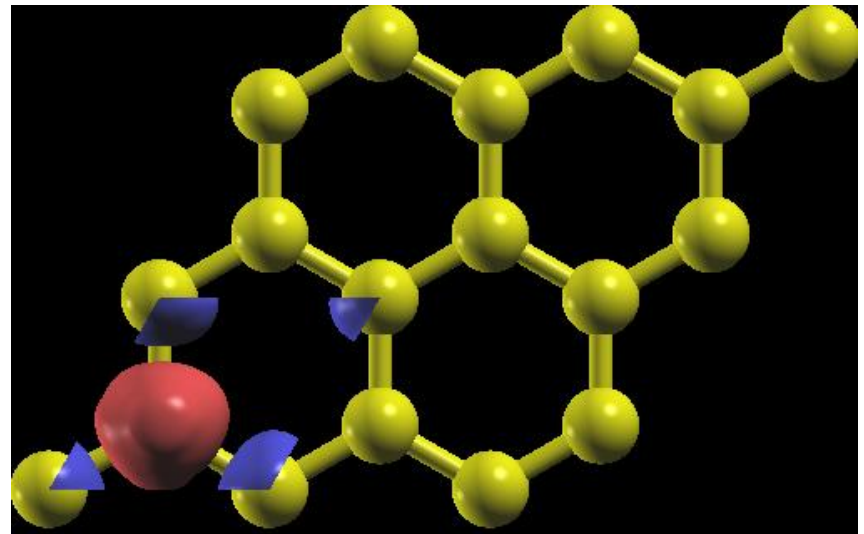
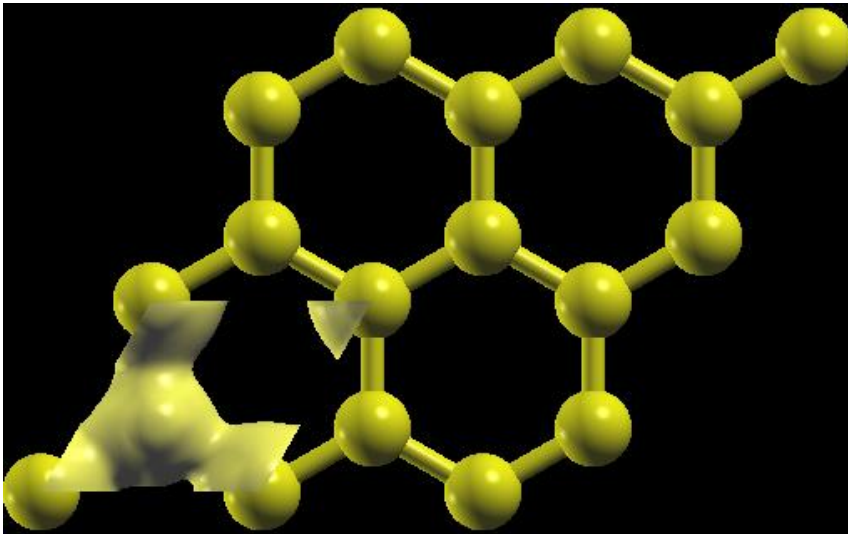
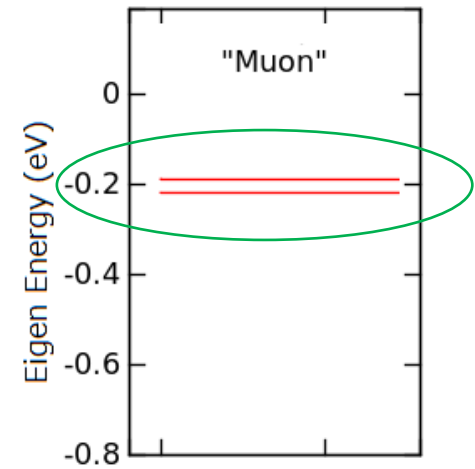
Adsorbed energy: **--0.22eV**

Split energy:  $\delta =$  **0.03eV**



# Wave function of muon in its ground state and 1<sup>st</sup> excited state

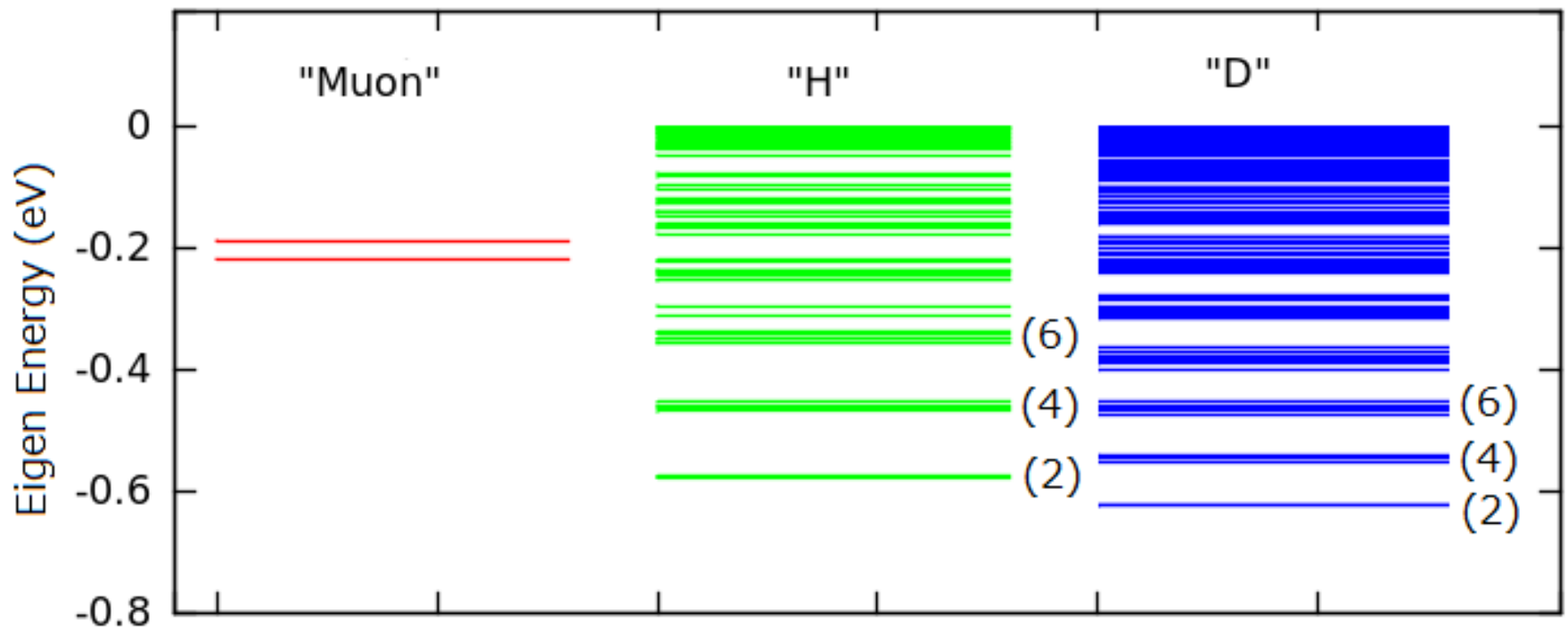
Adsorbed energy: **--0.22eV**  
Split energy:  $\delta =$  **0.03eV**



# Relaxed graphene

## Naniwa results

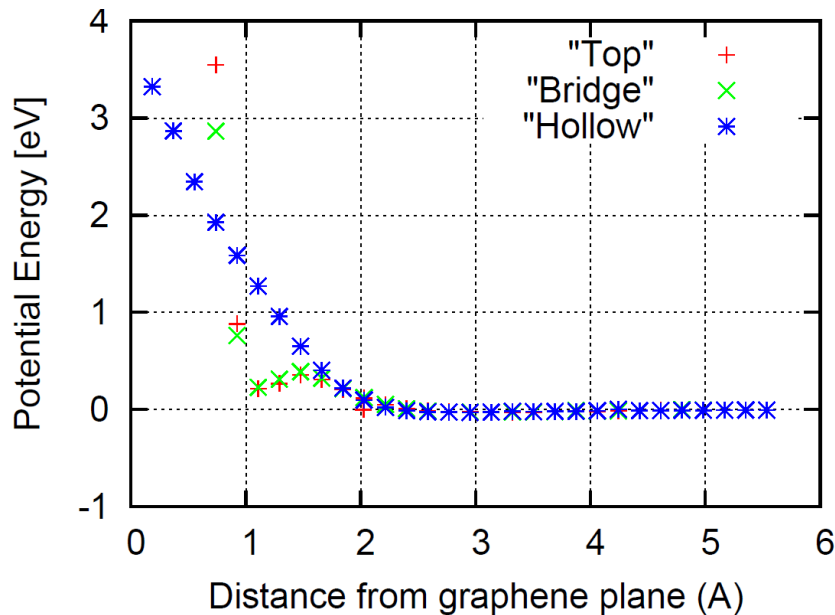
Eigen energies of positive muon, proton and deuteron on relaxed graphene



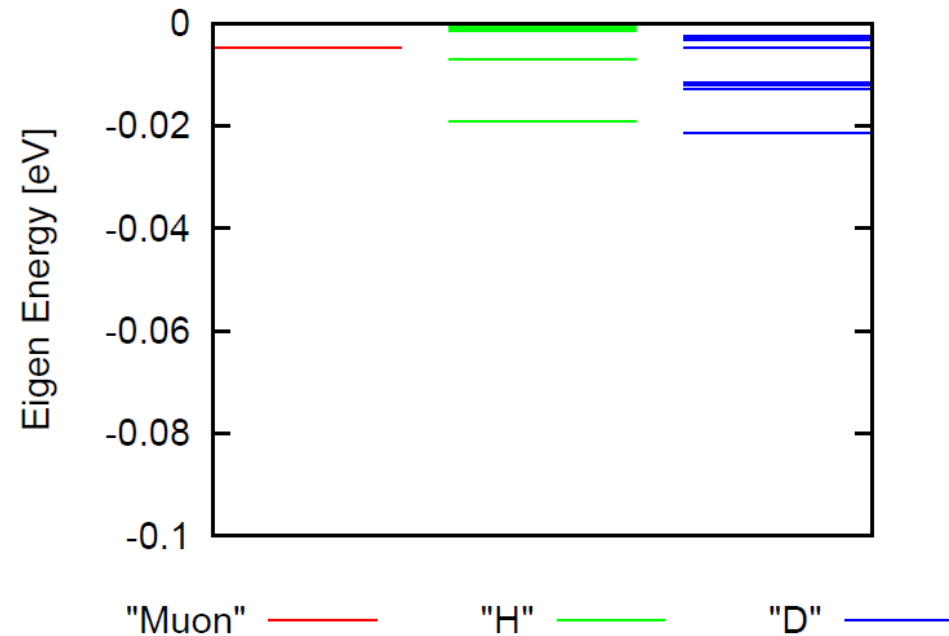
# Flat graphene

## Potential energy

Adiabatic potential energy calculation for hydrogen on fixed flat graphene



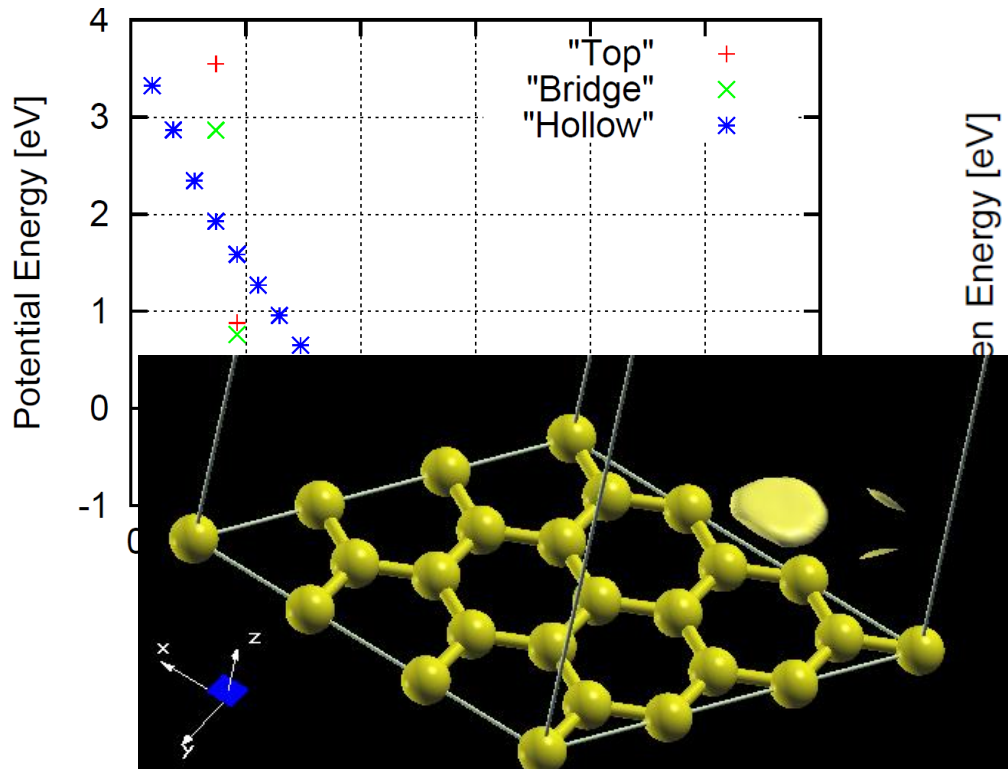
## Naniwa results



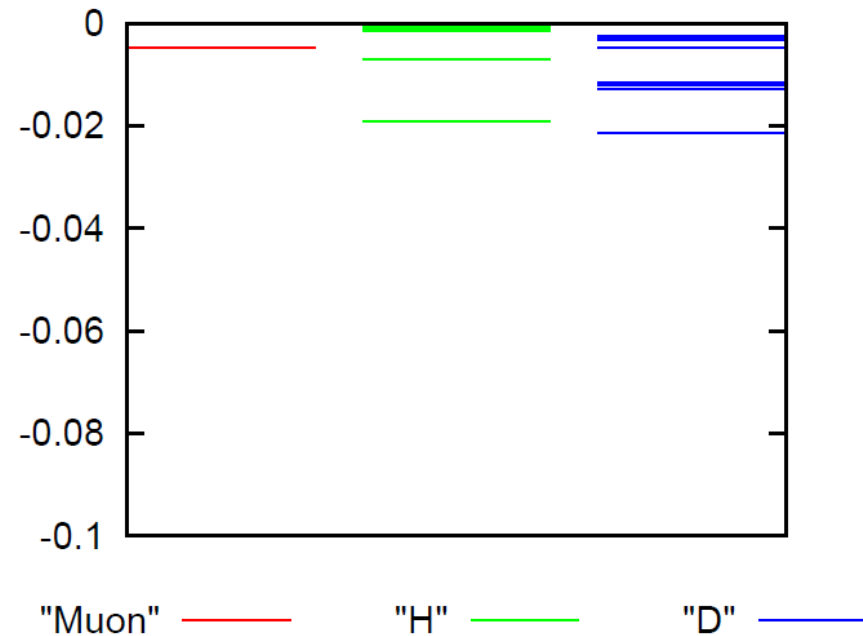
Eigen energies of positive muon, proton and deuteron on fixed flat graphene

# Flat graphene

## Potential energy



## Naniwa results



Eigen energies of positive muon,  
proton and deuteron on freezed  
graphene



# How about the charged states of particles

$$\langle n_{a \uparrow} + n_{a \downarrow} \rangle =$$

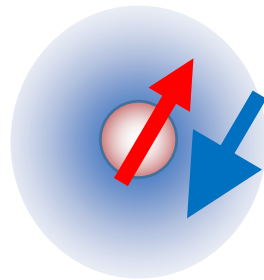
0,

1,

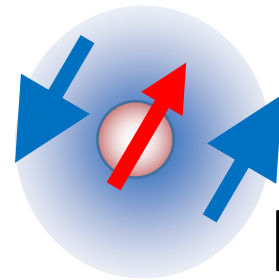
2



$H^+$



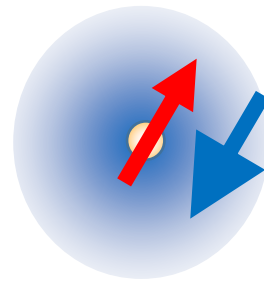
$H^0$



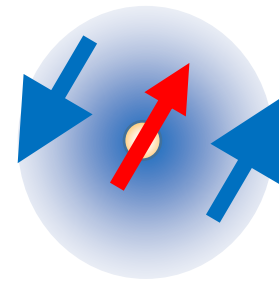
$H^-$



**Muon:  $\mu^+$**



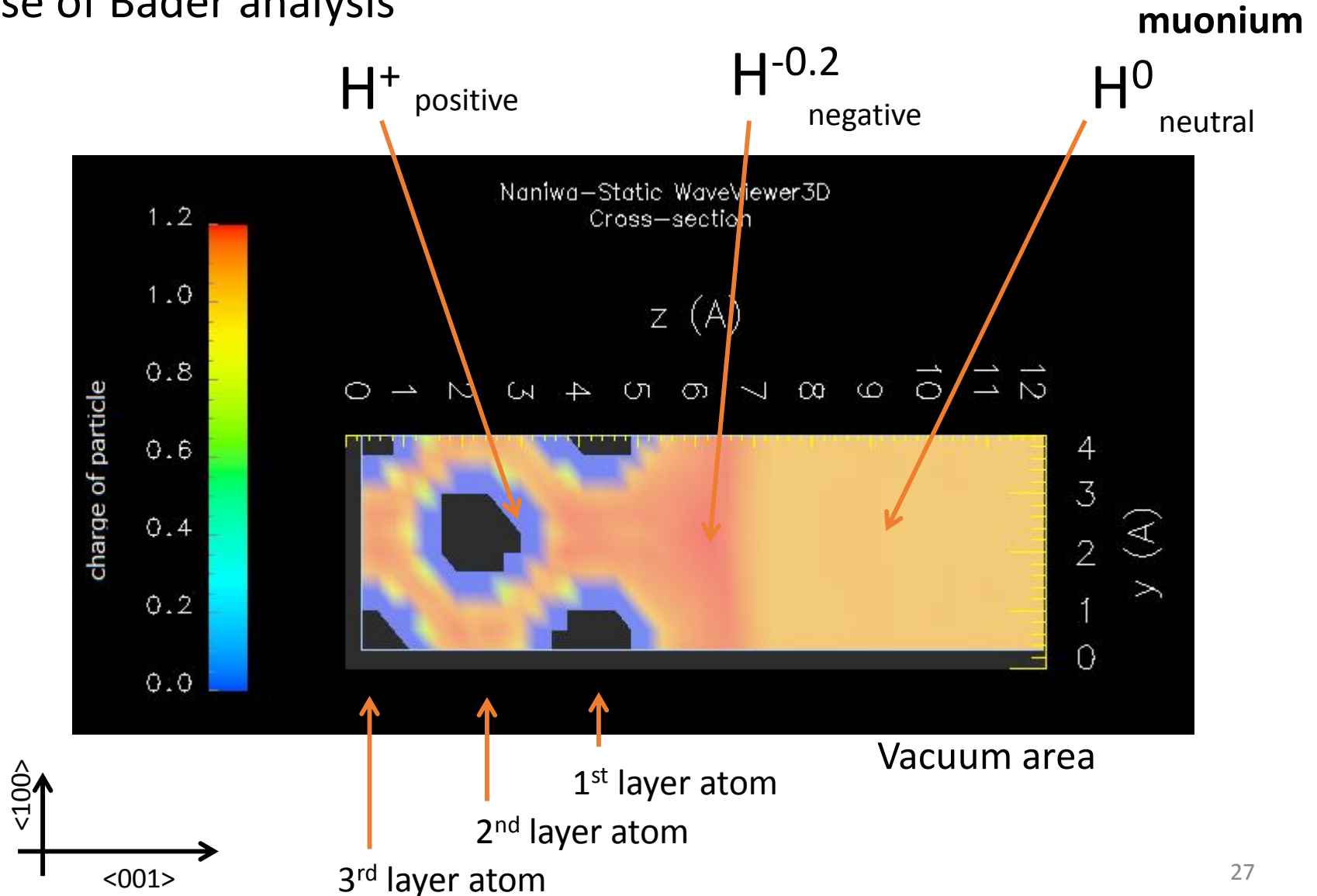
**Muonium:  $\mu^+ + e^-$**



**Negative ion :  $\mu^+ + 2e^-$**

# Charged states of target particle on Pd(001)

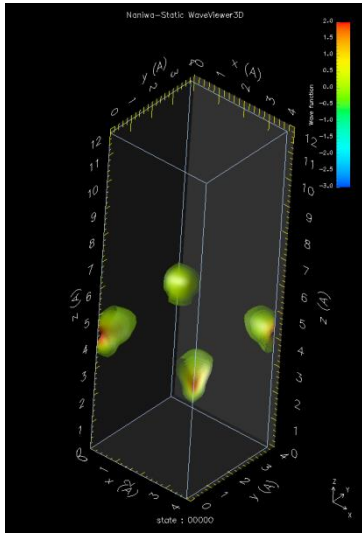
By use of Bader analysis



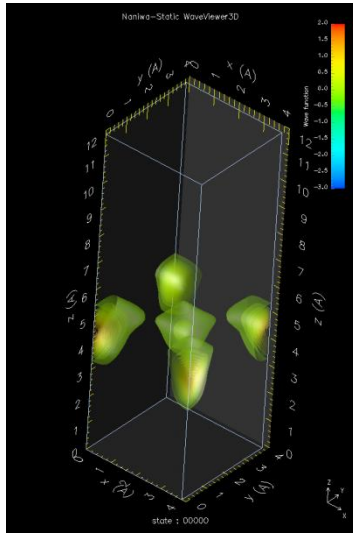
# Electron charge of the proton and anti-muon on Pd (001) surfaces



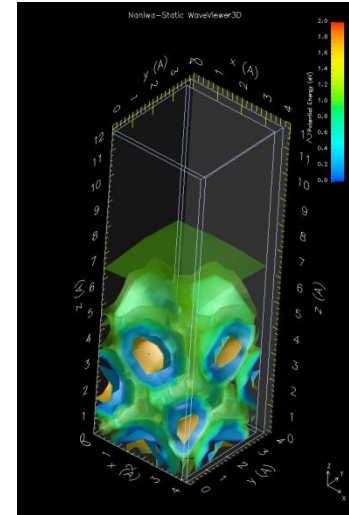
Ground state



$\Psi_0(\vec{R})$  for proton



$\Psi_0(\vec{R})$  for anti-muon



$$\iiint_{-\infty}^{+\infty} d\vec{r} \left\{ |\varphi_{a\uparrow}(\vec{r}; \vec{R})|^2 + |\varphi_{a\downarrow}(\vec{r}; \vec{R})|^2 \right\}$$

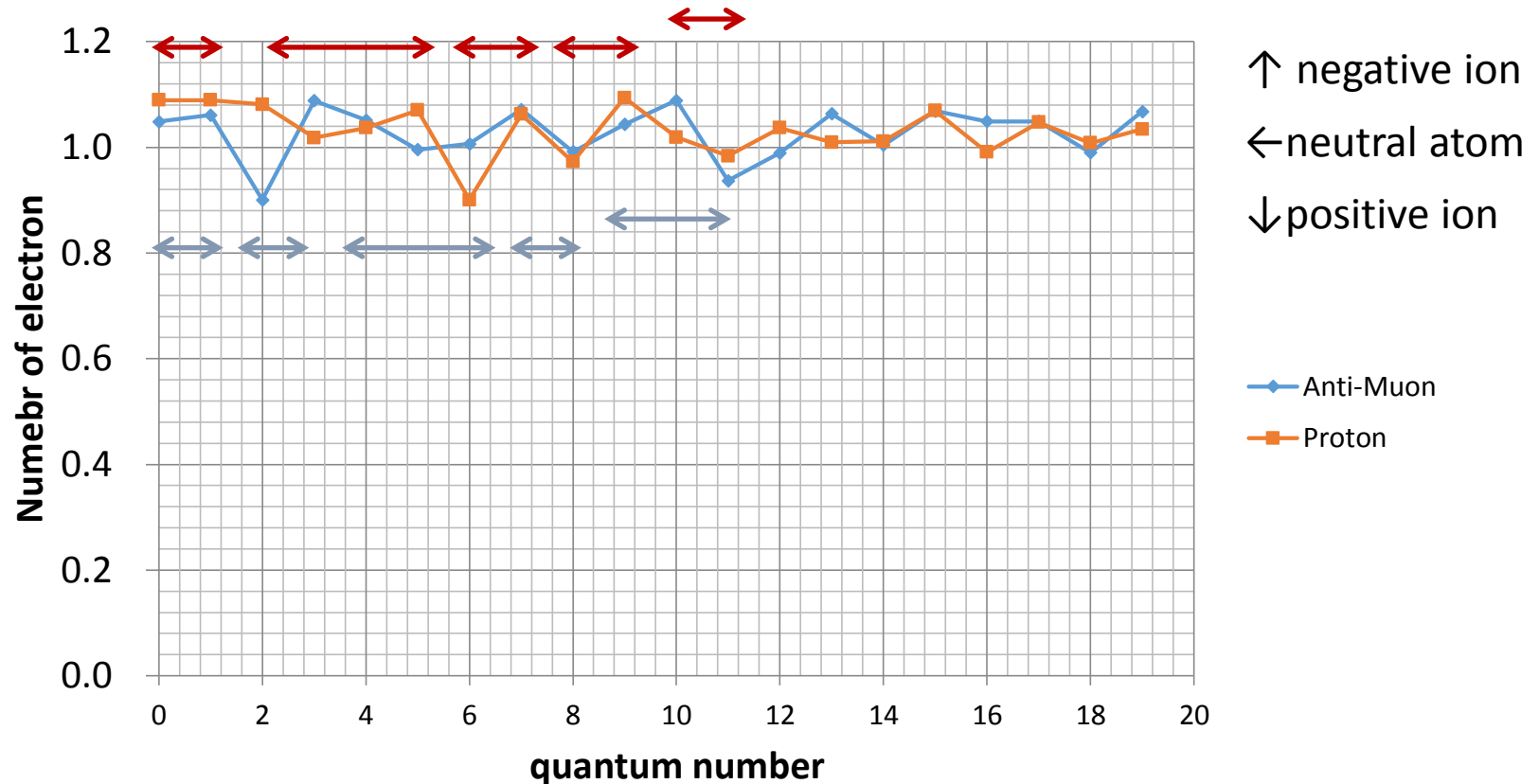
Expectation value of electron number on the particle'

$$\langle n_{a\uparrow} + n_{a\downarrow} \rangle_n = \iiint_{-\infty}^{+\infty} d\vec{R} \iiint_{-\infty}^{+\infty} d\vec{r} \left\{ |\varphi_{a\uparrow}(\vec{r}; \vec{R})|^2 + |\varphi_{a\downarrow}(\vec{r}; \vec{R})|^2 \right\} \cdot |\Psi_n(\vec{R})|^2$$

# Electron charge of target particle on Pd(001)

Ground state

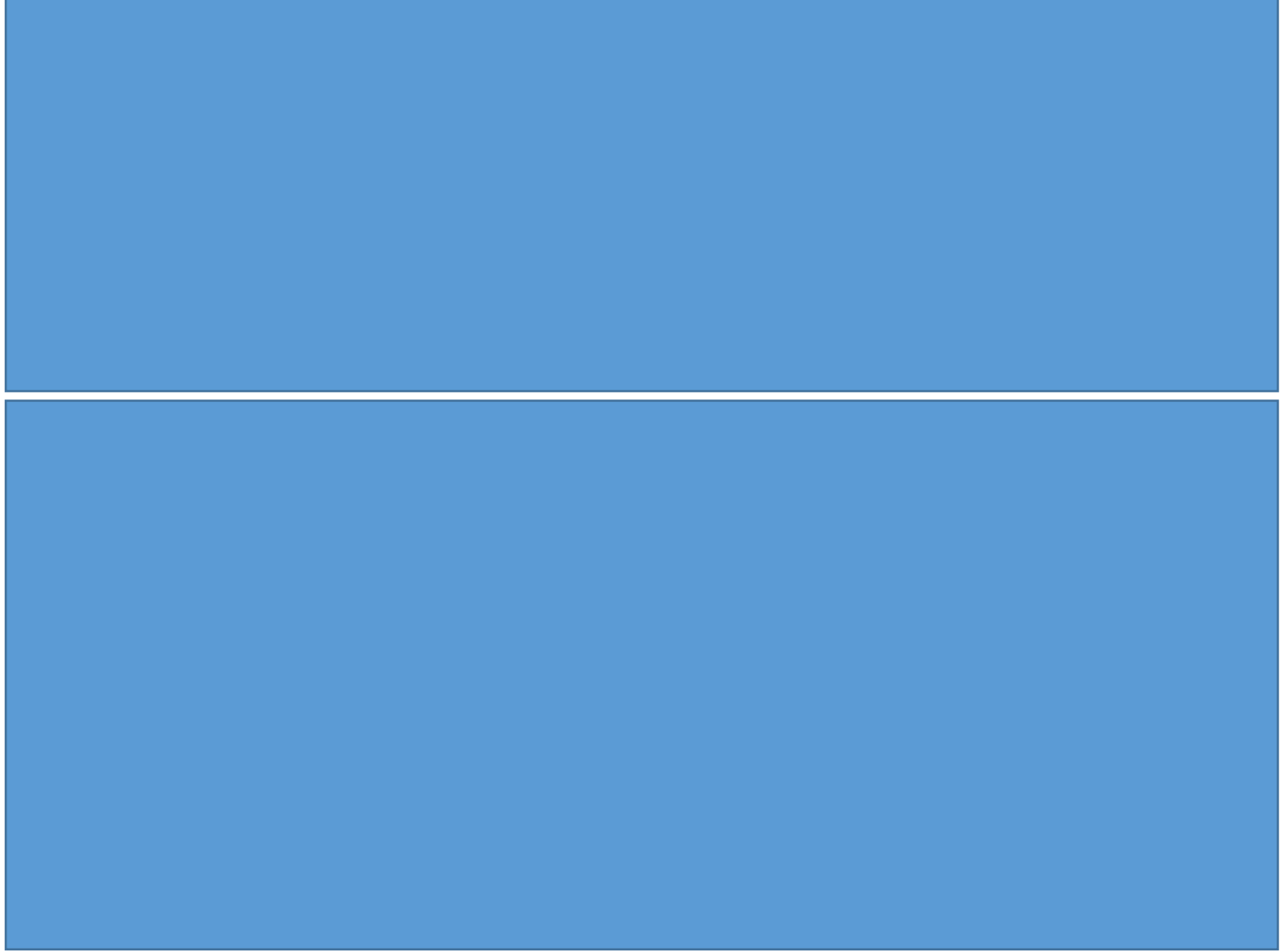
Core	Number of electron
(Anti)Muon	1.05
Proton	1.09



for  $\mu$ SR experiment

potential energy (eV)

超微細相互作用





# Summary

We have developing the parameter-free quantum simulation code “Naniwa: 浪速”

We investigate the quantum adsorbed states of positive muon ( $\text{Mu}^+$ ) and hydrogen atom nuclei ( $\text{H}^+$ ,  $\text{D}^+$ ) on graphene by our quantum simulation codes, Naniwa .

For hydrogen atom nuclei ( $\text{H}^+$ ,  $\text{D}^+$ )

The ground state wave function of hydrogen nucleus adsorbed on graphene is strongly localized at top site.

The adsorption energy is reduced from that expected by conventional DFT simulation. “It is more convenient for hydrogen storage usage.”

Vibrational excited states exist around this top site.

For positive muon ( $\text{Mu}^+$ )

There are only two adsorbed states, which are in their ground states.

No vibrational excited state.

Only the ground states can be measured by MuSR experiment.

\*We can estimate the hyperfine interactions, which is useful  
to know the state of hydrogen isotope on graphene.

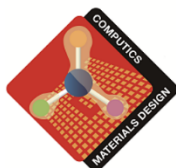
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文部科学省

Ministry of Education, Culture, Sports, Science  
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MEXT Science Research on Innovative Areas:



## Material Design through Computics:

Complex Correlation and Non-equilibrium Dynamics

**A02-7: New physical properties and quantum dynamics  
proved by protons and muons (22104008)**



## UltraSlow Muon Microscope

**A02: Spin transport and reactions at interface (23108003)**